

## Formation of xenon line profiles

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The characteristics of xenon line profiles in absorption spectra of inhomogeneous low-temperature plasma are investigated within the framework of the collision-radiant meta-equilibrium model. Broadening constants for xenon line profiles are calculated. The broadening mechanisms for xenon spectral lines are considered. Tabular data allowing determination of the electron concentrations from xenon line widths in the case of two-temperature meta-equilibrium plasma are presented.

### Introduction

Analysis of spectral line profiles of inert gas plasma is rather efficient in diagnostics for determination of parameters of the plasma under study. The problems of determination of plasma parameters from radiation characteristics are formally classified as inverse and ill-posed problems. The use of the calculated widths of xenon line profiles for diagnostic purposes<sup>1</sup> not always gives the desired result. The main difficulties are connected with two important problems, namely, variation of parameters of the plasma itself along the observation beam and the absence of theoretical recommendations in diagnostics of the thermally nonequilibrium two-temperature plasma.

The two-temperature quasi-stationary plasma possesses some features<sup>2,3</sup> distinguishing it from the thermally equilibrium plasma considered in the LTE model. The dependences described by the Saha–Boltzmann equations are violated. They are replaced with diagrams of meta-equilibrium states<sup>2,3</sup> being the results of solution of sublevel stationary kinetics. Such plasma is characterized by variation of the electron temperature  $T_e \approx (0.8 \pm 0.2)$  eV for the wide range of variation of the electron concentration  $N_e$  and the density of particles (number of nuclei).

In Ref. 2, we considered in detail the distribution of excited states of the two-temperature meta-equilibrium plasma<sup>3</sup> of inert gases. In this paper, the emphasis is on the photon distributions or line profiles in the case of meta-equilibrium xenon plasma.

### Broadening of spectral lines of xenon atom

To estimate the line widths of the two-temperature meta-equilibrium plasma, classic concepts are useful.<sup>4</sup> According to the collision theory, the main role in the broadening is played by particle transits within the Weiskopf radius

$$\rho_n = (\alpha_n C_n / v)^{1/(n-1)}. \quad (1)$$

Variation of the phase for the time of one collision can be written as

$$\eta = \int_{-\infty}^{\infty} \frac{C_n dt}{(\rho^2 + v^2 t^2)^{n/2}}. \quad (2)$$

Here  $C_n$  are the interaction constants;  $v$  is the mean speed of a flying particle;  $\alpha_n = \sqrt{\pi} \Gamma(n-1/2) \times \Gamma(n/2)$ ; and the collision width is

$$\gamma_n = 2\pi N_e v \rho_n. \quad (3)$$

The line broadening is affected by various interactions with charged and neutral particles, namely, the square Stark effect ( $n=4$ ), linear Stark effect ( $n=2$ ), van der Waals ( $n=6$ ), and resonance ( $n=3$ ) broadening.

For convenience, let us introduce the following designations, as in Ref. 5:

$$\bar{C}_3 = C_3 \cdot 10^8 \text{ (cm}^3/\text{s)}, \quad \bar{C}_4 = C_4 \cdot 10^{14} \text{ (cm}^4/\text{s)},$$

$$\bar{C}_6 = C_6 \cdot 10^{32} \text{ (cm}^6/\text{s)}. \quad (4)$$

The power parameters ( $T$ ,  $\hbar\omega$ ,  $\gamma$ ,  $\Delta$ , etc.) are expressed in electronvolts, and the concentrations are expressed in  $10^{18} \text{ cm}^{-3}$  ( $N_{e,a} = 10^{18} \cdot n_{e,a}$ ).

By the Weiskopf–Lindholm theory, the line width for the square Stark broadening can be presented as

$$\gamma_4 = 11.4 C_4^{2/3} v^{1/3} N_e; \quad (5)$$

$$\Delta_4 = 9.8 C_4^{2/3} v^{1/3} N_e. \quad (6)$$

The constant of square Stark broadening includes all transitions from a given level to upper and lower ones. Every transition was taken into account with its statistical weight  $g$ :

$$C_4 = \frac{e^4 \hbar}{4\pi m} \sum \frac{f}{(\hbar\omega)^2}, \quad C_{4(nl)} = \frac{1.18}{g_{nl}} \sum_{n'l'} \frac{gf(nl \rightarrow n'l')}{(\hbar\omega)_{nl,n'l'}^2}. \quad (7)$$

The final equations for the line width determined by the electron  $\gamma_{4,e}$  and ion  $\gamma_{4,i}$  impact take the form:

$$\gamma_{4,e} = 1.41 \cdot 10^{-3} n_e (\bar{C}_4)^{2/3} (T_e)^{1/6},$$

$$\gamma_{4,i} = 1.78 \cdot 10^{-4} n_i (\bar{C}_4)^{2/3} (T_i)^{1/6}. \quad (8)$$

The broadening of the line profile by neutral particles is taken into account in the van der Waals

mechanism. The interaction constant  $C_6$  is calculated most often by the approximate equation<sup>4</sup>:

$$C_6 = e^2 \alpha \bar{R}^2 / \hbar. \quad (9)$$

In Eq. (9),  $\alpha$  is the polarizability of the perturbed atom;  $\bar{R}^2$  is the mean squared radius of the orbit corresponding to the excited state of the emitting atom

$$\bar{R}^2 = a_0^2 n^{*2} \{5n^{*2} + 1 - 3l(l + 1)\} / (2Z), \quad (10)$$

where  $n^*$  is the effective quantum number;  $l$  is the orbital moment. After transformation (7) we have

$$\bar{C}_6 = 0.391 \frac{n^{*2}}{2Z} \{5n^{*2} + 1 - 3l(l + 1)\}. \quad (11)$$

The line width in this case is

$$\gamma_6 = 1.02 \cdot 10^{-6} (\bar{C}_6)^{2/5} (T_a)^{3/10} n_a \quad (12)$$

and the shift is

$$\Delta_6 = 2.96 C_6^{2/5} v^{3/5} N_a. \quad (13)$$

The resonance broadening is practically significant only for the transitions involving the ground state.<sup>5</sup> The line width  $\gamma_3$  is connected with the oscillator strength  $f_{abs}$  by the equation

$$\gamma_3 = 4 \frac{e^2 f_{abs}}{m \hbar \omega} N_a \sqrt{\frac{2J_0 + 1}{2J_1 + 1}}, \quad (14)$$

where  $N_a$  is the concentration of atoms;  $J_0$  and  $J_1$  are the total moments of the atom in the ground ( $5p^{61}S_0$ ) and excited ( $5p^5ns$ ,  $5p^5nd$ ) states involved in the main dipole transition ( $J_1 = 1$ ). According to Eqs. (1) and (2), we have

$$\gamma_3 = 2\pi\alpha_3 C_3 N_a, \quad (15)$$

where

$$C_3 = 3.05 \cdot 10^{-8} f_{abs} / \hbar\omega. \quad (16)$$

Then the equations for calculation of the line width  $\gamma_3$  take the form

$$\gamma_3 = 8.33 \cdot 10^{-5} n_a \bar{C}_3. \quad (17)$$

It should be noted that the resonance broadening, unlike other mechanisms, is independent of temperature.

Table 1 gives the calculated energy levels and constants  $\bar{C}_3$ ,  $\bar{C}_4$ , and  $\bar{C}_6$  (Ref. 6).

The line width is determined as

$$\gamma = \gamma_{4e} + \gamma_{(\sigma v)} + \gamma_3 + \gamma_6, \quad (18)$$

where  $\gamma_{(\sigma v)}$  is the width caused by inelastic collisions with electrons.<sup>5</sup>

The experimentally measured xenon line widths obtained from the spectra reported in Ref. 10 and those calculated theoretically by Eq. (18) are given in Table 2. It should be noted that some values for the  $s$ - $p$ -transitions coincide or differ approximately two times. For the  $d$ -states, the most probable decay channel of the molecular ion, the widths of the  $p$ - $d$ -transitions differ ten times.

**Table 1. Values of the main quantum numbers, energy levels, and broadening constants  $\bar{C}_3$ ,  $\bar{C}_4$ , and  $\bar{C}_6$**

#	Level	$n^*$	$E$ , eV	$\bar{C}_3$	$\bar{C}_4$	$\bar{C}_6$
1	6s[3/2] <sub>1</sub>	1.919296	8.436	14	0.75	14
2	7s[3/2] <sub>1</sub>	2.975527	10.592	78	12.1	78
3	8s[3/2] <sub>1</sub>	3.987458	11.274	250	60	250
4	6s[3/2] <sub>2</sub>	1.888554	8.315	-	0.6	13
5	7s[3/2] <sub>2</sub>	2.945823	10.561	-	8.4	75
6	8s[3/2] <sub>2</sub>	3.951016	11.257	-	21	240
7	6p[1/2] <sub>0</sub>	2.488849	9.932	-	-15	32
8	7p[1/2] <sub>0</sub>	3.493408	11.014	-	-27	130
9	8p[1/2] <sub>0</sub>	4.559365	11.475	-	-	400
10	6p[1/2] <sub>1</sub>	2.309966	9.579	-	1.8	23
11	7p[1/2] <sub>1</sub>	3.328154	10.901	-	44	110
12	8p[1/2] <sub>1</sub>	4.395120	11.425	-	-	350
13	6p[3/2] <sub>1</sub>	2.410965	9.789	-	2.6	27
14	7p[3/2] <sub>1</sub>	3.474583	11.002	-	60	130
15	8p[3/2] <sub>1</sub>	4.466373	11.447	-	-	370
16	6p[3/2] <sub>2</sub>	2.427514	9.82	-	3.7	28
17	7p[3/2] <sub>2</sub>	3.463531	10.995	-	470	130
18	8p[3/2] <sub>2</sub>	4.481798	11.452	-	-	375
19	6p[5/2] <sub>2</sub>	2.359279	9.685	-	2	25
20	7p[5/2] <sub>2</sub>	3.401835	10.953	-	53	120
21	8p[5/2] <sub>2</sub>	4.421704	11.433	-	-	355
22	6p[5/2] <sub>3</sub>	2.376416	9.72	-	2.3	26
23	7p[5/2] <sub>3</sub>	3.423111	11.005	-	80	120
24	8p[5/2] <sub>3</sub>	4.43898	11.432	-	-	360
25	5d[1/2] <sub>0</sub>	2.464777	9.89	16	1.3	16
26	6d[1/2] <sub>0</sub>	3.427102	10.97	96	-15	96
27	7d[1/2] <sub>0</sub>	4.436948	11.438	310	-280	310
28	5d[1/2] <sub>1</sub>	2.47967	9.917	17	4.8	17
29	6d[1/2] <sub>1</sub>	3.437937	10.978	97	36	97
30	7d[1/2] <sub>1</sub>	4.385481	11.42	300	1400	300
31	5d[3/2] <sub>1</sub>	2.805277	10.4	34	0.94	34
32	6d[3/2] <sub>1</sub>	3.750338	11.162	150	24	150
33	7d[3/2] <sub>1</sub>	4.629578	11.495	375	-110	375
34	5d[3/2] <sub>2</sub>	2.496709	9.958	17	-1.8	17
35	6d[3/2] <sub>2</sub>	3.467703	10.998	100	-450	100
36	7d[3/2] <sub>2</sub>	4.632927	11.495	380	-5	380
37	5d[5/2] <sub>2</sub>	2.626362	10.157	24	-0.8	24
38	6d[5/2] <sub>2</sub>	3.574013	11.064	120	-12	120
39	7d[5/2] <sub>2</sub>	4.613565	11.49	370	-40	370
40	5d[5/2] <sub>3</sub>	2.669041	10.219	26	-0.7	26
41	6d[5/2] <sub>3</sub>	3.636195	11.112	130	0.1	130
42	7d[5/2] <sub>3</sub>	4.638419	11.5	380	-30	380
43	5d[7/2] <sub>3</sub>	2.550903	10.039	20	-0.9	20
44	6d[7/2] <sub>3</sub>	3.52943	11.037	110	-14	110
45	7d[7/2] <sub>3</sub>	4.599136	11.486	370	-33	370
46	5d[7/2] <sub>4</sub>	2.494325	9.943	17	-1.4	17
47	6d[7/2] <sub>4</sub>	3.506969	11.023	107	-31	107
48	7d[7/2] <sub>4</sub>	4.512464	11.461	340	-3800	340
49	6s'[1/2] <sub>0</sub>	1.846778	9.445	-	0.6	11
50	7s'[1/2] <sub>0</sub>	2.945265	11.865	-	14	72
51	8s'[1/2] <sub>0</sub>	3.945265	12.559	-	79	230
52	6s'[1/2] <sub>1</sub>	1.875812	9.568	23	0.6	11
53	7s'[1/2] <sub>1</sub>	2.954575	11.875	110	19	72
54	8s'[1/2] <sub>1</sub>	3.974836	12.572	350	80	240
55	6p'[1/2] <sub>0</sub>	2.434749	11.139	-	2.6	29
56	7p'[1/2] <sub>0</sub>	3.434749	12.28	-	33	125
57	8p'[1/2] <sub>0</sub>	4.434749	12.741	-	210	360
58	6p'[1/2] <sub>1</sub>	2.397397	11.067	-	2.7	24
59	7p'[1/2] <sub>1</sub>	3.397397	12.255	-	44	110
60	8p'[1/2] <sub>1</sub>	4.397397	12.73	-	280	330
61	6p'[3/2] <sub>1</sub>	2.342837	10.955	-	3.3	24
62	7p'[3/2] <sub>1</sub>	3.342837	12.216	-	34	110

Table 1 (continued)

#	Level	$n^*$	$E, \text{ eV}$	$\bar{C}_3$	$\bar{C}_4$	$\bar{C}_6$
63	$8p'[3/2]_1$	4.342837	12.712	–	230	330
64	$6p'[3/2]_2$	2.390129	11.052	–	2.8	26
65	$7p'[3/2]_2$	3.390129	12.25	–	260	120
66	$8p'[3/2]_2$	4.390129	12.727	–	260	340
67	$5d'[3/2]_1$	2.727304	11.605	–	–4.1	29
68	$6d'[3/2]_1$	3.714424	12.449	–	–0.1	140
69	$7d'[3/2]_1$	4.707171	12.821	–	130	405
70	$5d'[3/2]_2$	2.546386	11.337	–	–11	20
71	$6d'[3/2]_2$	3.546386	12.354	–	–8	110
72	$7d'[3/2]_2$	4.546386	12.777	–	–70	350
73	$5d'[5/2]_2$	2.524493	11.3	–	–0.8	19
74	$6d'[5/2]_2$	3.524493	12.34	–	–21	110
75	$7d'[5/2]_2$	4.524493	12.771	–	–160	340
76	$5d'[5/2]_3$	2.569191	11.374	–	–0.1	21
77	$6d'[5/2]_3$	3.569191	12.372	–	–3.6	115
78	$7d'[5/2]_3$	4.569191	12.784	–	–43	360

The technique of measurement of the electron concentration  $N_e$  from the width of a spectral line of inert gases does not lose its urgency within the framework of the model of meta-equilibrium plasma. (Remind that the value of  $N_e$  obtained in such a way may fail meeting the Saha–Boltzmann equations.) For  $N_e \geq 10^{16} \text{ cm}^{-3}$  the line width is proportional to the electron concentration. At  $N_e < 10^{16} \text{ cm}^{-3}$  the contribution of the van der Waals collisional broadening is significant. Its value is proportional to the concentration of atoms. To determine the electron concentration, we should subtract the van der Waals component  $\gamma_6$  proportional to the concentration of atoms from the width of the line under study (18).

Table 3 gives the line widths of the Xe atom caused by different broadening mechanism and related to one atom (electron):  $\gamma_{4e}/n_e$ ,  $\gamma_{\langle\sigma v\rangle}/n_e$ ,  $\gamma_6/n_a$ , and  $\gamma_3/n_a$  for the temperature  $T_e = 0.5, 0.7, \text{ and } 0.9 \text{ eV}$ .

Table 3. Values of  $\gamma_{4e}/n_e$ ,  $\gamma_{\langle\sigma v\rangle}/n_e$ ,  $\gamma_6/n_a$ , and  $\gamma_3/n_a$  for the temperature  $T_e = 0.5, 0.7, \text{ and } 0.9 \text{ eV}$

Transition $\lambda, \text{ \AA}$	$T_e, \text{ eV}$	$\gamma_{4e}/n_e, \text{ eV/cm}^{-3}$	$\gamma_{\langle\sigma v\rangle}/n_e, \text{ eV/cm}^{-3}$	$\gamma_6/n_a, \text{ eV/cm}^{-3}$	$\gamma_3/n_a, \text{ eV/cm}^{-3}$
$6s[3/2]_1 \rightarrow 6p[1/2]_0$ 8279.9	0.5	0.0074	0.0108	5.69E-06	3.96E-6
	0.7	0.008	0.0104	6.1 E-06	4.0 E-6
	0.9	0.0082	0.0092	6.75E-06	4.19E-6
$6s[3/2]_1 \rightarrow 7p[1/2]_0$ 4806.9	0.5	0.0111	0.0286	1.06E-05	3.96E-6
	0.7	0.0121	0.0282	1.19E-05	4.0 E-6
	0.9	0.0126	0.028	1.29E-05	4.19E-6
$6s[3/2]_{1,2} \rightarrow 7p[1/2]_1$ 5028.1; 4792.5	0.5	0.0156	0.0187	1.03E-05	3.96E-6
	0.7	0.0168	0.0177	1.13E-05	4.0 E-6
	0.9	0.0173	0.0166	1.28E-05	4.19E-6
$6s[3/2]_{1,2} \rightarrow 7p[3/2]_1$ 4829.6; 4611.8	0.5	0.0188	0.0412	1.07E-05	3.96E-6
	0.7	0.0196	0.0313	1.29E-05	4.0 E-6
	0.9	0.0204	0.026	1.28E-05	4.19E-6
$6s[3/2]_{1,2} \rightarrow 7p[3/2]_2$ 4843.2; 4624.1	0.5	0.0926	0.0861	1.07E-05	3.96E-6
	0.7	0.0966	0.0929	1.19E-05	4.0 E-6
	0.9	0.1019	0.1066	1.29E-05	4.19E-6
$6s[3/2]_{1,2} \rightarrow 7p[5/2]_2$ 4923.0; 4696.9	0.5	0.0231	0.0477	1.06E-05	3.96E-6
	0.7	0.0257	0.0446	1.18E-05	4.0 E-6
	0.9	0.0257	0.0456	1.28E-05	4.19E-6
$6s[3/2]_2 \rightarrow 7p[5/2]_3$ 4671.1	0.5	0.0257	0.0258	1.05E-05	0
	0.7	0.0276	0.0270	1.16E-05	0
	0.9	0.0278	0.0208	1.25E-05	0

Note. 5.69E-06 means  $5.96 \cdot 10^{-6}$  and so on.

These values correspond to the slope of a straight line on the plot of the line width dependence on the electron concentration  $\gamma = \gamma(N_e)$ . Given the experimental width, we can determine the electron concentration ( $\gamma = \frac{1.24 \cdot 10^4}{\lambda^2} \Delta\lambda$ , where  $\gamma$  is expressed in eV, and  $\lambda$  and  $\Delta\lambda$  are given in  $\text{\AA}$ ).

Table 2. Experimental values of the shift  $\delta$ , width  $\gamma$ , ratio  $\gamma/\delta$  from Ref. 10 and our calculation by Eq. (18), in  $10^{-7} \text{ eV}$ ;  $N_e \sim 6 \cdot 10^{13} \text{ cm}^{-3}$

Transition	$\lambda, \text{ nm}$	$\delta_{\text{exp}}$	$\gamma_{\text{exp}}$	$\frac{\gamma_{\text{exp}}}{\delta_{\text{exp}}}$	$\gamma$ (18)
$6s[3/2]_1 \rightarrow 6p[1/2]_0$	827.99	–2.5(0.5)*	5(0.6)	20	4.8
$6s[3/2]_1 \rightarrow 6p[3/2]_2$	895.2	1.2(0.2)	5.(0.1)	4.2	4.5
$6s[3/2]_1 \rightarrow 6p[3/2]_1$	916.24	0.6(0.2)	–	–	4.8
$6s[3/2]_2 \rightarrow 6p[3/2]_2$	823.1	0.(0.3)	$\leq 2.5(2.0)$	–	2.8
$6s[3/2]_2 \rightarrow 6p[3/2]_1$	840.89	0.5(0.2)	1.24(0.7)	2.5	3.4
$6s[3/2]_2 \rightarrow 6p[3/2]_3$	881.91	0.12(0.5)	$\leq 2.5(2.0)$	21.0	2.5
$6s[3/2]_2 \rightarrow 6p[5/2]_2$	904.51	0.37(0.2)	1.25(0.8)	3.4	2.4
$6s[3/2]_1 \rightarrow 7p[1/2]_0$	480.69	1.(0.3)	5.(2.0)	5.0	7.8
$6s[3/2]_1 \rightarrow 7p[3/2]_1$	482.96	1.(1.)	7.5(2.0)	7.5	9.3
$6s[3/2]_1 \rightarrow 7p[3/2]_2$	484.32	2.5(0.2)	7.5(3.0)	3.0	17.0
$6s[3/2]_1 \rightarrow 7p[5/2]_2$	492.3	1.6(0.4)	7.5(2.0)	4.7	9.5
$6s[3/2]_2 \rightarrow 7p[3/2]_2$	462.41	2.4(0.3)	7.5(1.5)	3.1	15.0
$6s[3/2]_2 \rightarrow 7p[5/2]_3$	467.11	2.(0.4)	7.5(2.0)	3.8	7.4
$6s[3/2]_2 \rightarrow 7p[5/2]_2$	469.69	2.1(0.25)	5.(2.0)	2.4	8.1
$6s[1/2]_1 \rightarrow 6p[1/2]_1$	826.6	1.(0.1)	3.7(0.5)	3.7	3.2
$6s[1/2]_1 \rightarrow 6p[3/2]_2$	834.66	0.5(0.2)	3.7(1.0)	7.4	3.3
$6p[1/2]_1 \rightarrow 6d[3/2]_2$	873.91	0.25(0.1)	5.(0.6)	20.0	48.0
$6p[1/2]_1 \rightarrow 6d[1/2]_0$	890.84	1.24(0.5)	3.7(0.6)	3.0	7.4
$6p[1/2]_1 \rightarrow 7d[3/2]_2$	646.95	1.5(0.2)	7.5(0.7)	5.0	40.0
$6p[1/2]_1 \rightarrow 7d[3/2]_1$	647.26	1.5(0.6)	6.2(4.0)	4.1	40.0
$6p[3/2]_1 \rightarrow 7d[5/2]_2$	728.51	1.6(0.3)	7.5(0.7)	4.7	40.0

\* The minus sign means the blue shift; the value in parenthesis is the relative measurement error.

## Spectral line profile of cylindrical plasma column with variable electron concentration

In Ref. 7, the “method of localizations” was proposed, which allows the local emissivity of plasma of inhomogeneous objects possessing the axial symmetry to be determined without using traditional inversion methods. This method was based on the fact that the plasma emissivity decreases fast with temperature drop at a constant pressure, and, as a consequence, the total emission, measured experimentally, is mostly caused by the axial zones of a plasma body.

Reference 7 considers an inhomogeneous plasma body, the pressure in which is constant and the temperature distribution along the observation line is symmetric and has the parabolic shape.

In numerical simulation, the formal solution of the transfer equation

$$I_{\lambda}(\tau) = I_{\lambda}(0)\exp(-\tau) + \int_0^{\tau} I_{\lambda P}(\tau')\exp(\tau' - \tau)d\tau';$$

$$\tau = \int_y^{\infty} x_{\lambda}(y')dy' \quad (19)$$

is used to determine the radiation intensity. A numerical algorithm reduces the solution to the recurrent equation relating the radiation intensity at neighboring points:

$$I_{\lambda}(\tau_i) = I_{\lambda}(\tau_{i-1})\exp(-\Delta\tau_i) + I_{\lambda P}(\tau_i) \times [1 - \exp(-\Delta\tau_i)] - \left(\frac{dI_{\lambda P}}{d\tau}\right)_i [1 - \exp(-\Delta\tau_i)(1 + \Delta\tau_i)]. \quad (20)$$

The spectral absorption coefficient  $x_{\lambda}$  has the form

$$x_{\lambda} = \pi e^2 f_{nm} N_e \phi(\lambda) / (mc). \quad (21)$$

Since the central part of the profile is caused by collisions with electrons, the profile is a Lorentzian one with the halfwidth  $\gamma/2$  and the shift  $\delta$  proportional to the electron concentration and weakly dependent on the temperature.

In the non-traditional part of the diagram of meta-equilibrium states of the inert gas plasma, we have another situation: the electron temperature varies insignificantly, and the electron concentration, for example, over the radius of the cylindrical column may decrease by an order of magnitude.

Let us specify the decrease of the electron concentration over the radius ( $r = 1$  cm) as is shown in Fig. 1 (curve 1) or assume that it is constant (curve 2). Then consider the profile of the line corresponding to the transition  $6s[3/2]_1 \rightarrow 7p[1/2]_0$  in absorption at  $\lambda = 4810.9 \text{ \AA}$  XeI. The line width is caused, as in the above case, by the square Stark effect, and the constant is  $C_4 = -27 \cdot 10^{-14} \text{ cm}^4 \cdot \text{s}^{-1}$  (blue shift). The calculations are carried out formally by Eqs. (19)–(21) in the very simplified version for four cases:

1)  $N_e$  is specified according to curve 1 (see Fig. 1) and the lower level population and temperature are determined from solution of equations of the sublevel kinetics for the xenon plasma<sup>8</sup> at the given number of nuclei (diagrams of meta-equilibrium states of Xe);

2)  $N_e$  is specified according to curve 1 and the lower level population and temperature are calculated using the Saha–Boltzmann equations at known  $N_e$  and the density;

3)  $N_e = \text{const}$ , the lower level population and the temperature are determined from solution of the equations of sublevel kinetics;

4)  $N_e = \text{const}$ , the lower level population and the temperature are calculated using the Saha–Boltzmann equations at known  $N_e$  and the density.

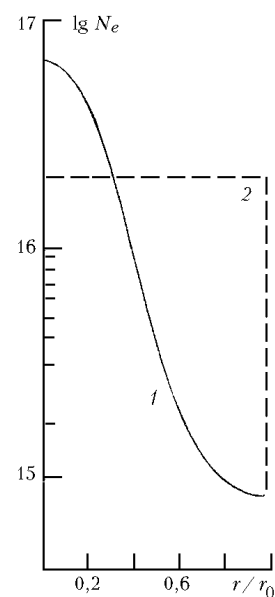


Fig. 1. Distribution of electron concentration over the radius.

Figure 2 shows the profile of the line at  $\lambda = 4810.9 \text{ \AA}$  XeI for the cases listed above. The first two cases are shown in Fig. 2a, the third case for  $N_e = 2 \cdot 10^{16} \text{ cm}^{-3}$  corresponds to curve 1 in Fig. 2b, and the fourth case corresponds to curve 2.

Curve 2 in Fig. 2a is obtained in the same way as the profiles in Ref. 7 and is asymmetric as well. Curve 1 in this figure has an unusual shape. The similar shape was observed in Ref. 9, which presented a microphotogram (shown in Fig. 2c) for the argon plasma in the spark discharge (curve 1). This shape is compared with curve 2 corresponding to the spectrum of hollow cathode plasma (plasma parameters differ insignificantly). The left line in the microphotogram 2 coincides with the peak of curve 1 (Fig. 2c), i.e., the transition wavelength is the same in the first and the second cases. However, the left peak is complemented with a second “wide line.” Actually, the peak and the “wide line” form the profile of one transition, whose behavior is similar to curve 1 in Fig. 2a (shifts are different because of the sign of the constant  $C_4$ ).

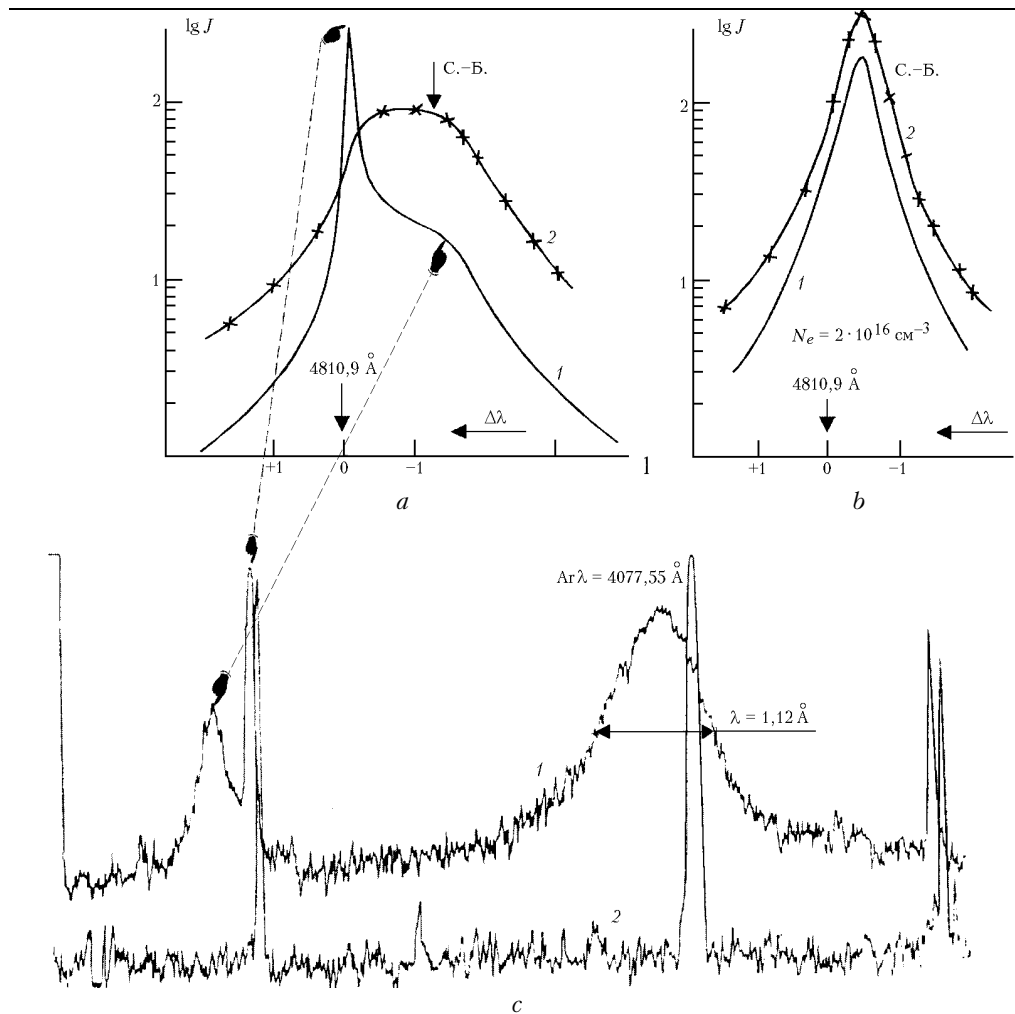


Fig. 2. Calculated intensity of XeI line at  $\lambda = 4077.55 \text{ \AA}$  (a, b) (Saha–Boltzmann), microphotogram of ArII lines,<sup>9</sup> arrows show the identity in the profile behavior (c).

## Conclusion

As a result of numerical solution of the system of equations of sublevel kinetics, we have obtained the diagrams of meta-equilibrium states of inert gas plasma that establish one-to-one correspondence between the electron concentration, gas density, and the given electron temperature. The meta-equilibrium states are characterized by the distributions of the excited states different from the Boltzmann distribution and having the shape of a polyline.

The characteristics of line profiles in absorption spectra of the inhomogeneous low-temperature plasma have been studied in the case that the electron concentration decreases over the radius by an order of magnitude and even more. The mechanisms of broadening of spectral lines have been studied for the meta-equilibrium plasma. The tabulated data are presented that allow estimating for the case of the meta-equilibrium plasma. Recommendations for diagnostics of plasma are given.

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